Influence in Social Networks

The social networks have grown at an unprecedented level in the last decade where millions of people interact at any given time. Social network has become so pervasive in a way that they could influence the behaviour of individuals and groups that it has led to much research in many areas, particularly information diffusion. It refers to spread of information, through “word of mouth” propagation among friends in social network. Information diffusion has attracted extensive research from many areas including physics [1], economics [2], computer science [3], [4], sociology [5], epidemiology [17] and health [15]. Many applications of where information spread is studies include viral marketing [5], network monitoring [6], rumour control [7], influential spreader in social network [14], social recommendation [8] and causal analysis [16].

A main algorithmic problem in information diffusion is influence maximization (IM). Main goal of IM is to select a set of k users in online social network, (seed set) with the maximum influence spread (i.e. is the maximum no of individuals influenced when the seed set is maximized). The problem was first modelled as probalistic model of interaction with heuristics [9] for choosing the best seeds and then as a discrete optimization problem[3],[4]. Despite many applications of IM it faces many challenges. First is modelling the information diffusion in social network that would heavily affect the influence of any seed set in IM. Second IM problem is computationally intractable. It has been shown that obtaining an optimal solution is NP-Hard [3]. Although a greedy solution has been proposed that achieves 1-1/e approximation [3]. Third, due to random nature of social networks, even evaluation of information spread of an individual seed is computationally complex. Fourth, identifying the influence can be challenging as Individuals tend to engage in similar activities as their peers, so it is often impossible to determine from observational data whether a correlation between two individuals’ behaviours exists because they are similar or because one person’s behaviour has influenced the other. [16]

With various research in optimization framework of IM various solutions have been proposed, that reduces the run time of the original greedy algorithm [10-12]. Also there has been research to improve that have included network assortavity that have improved that has led to increase in the influence propagation as compared to baseline models. [13]. There have been various models proposed in the literature to model the influence maximization problem, including linear threshold model (LT), independent cascade model (IC), triggering model (TR), time aware diffusion models and non-progressive diffusion models [24], with the most popular being LT and IC.

Threshold model assume that there exists a threshold value for node or people at which they adopt the product or behaviour. In the simplest of these models, the LT model each node v has a latent threshold θ(v) and for every neighbour u∈ N(v) (where N(v) is set of neighbours in the graph) (u,v) has a non-negative weight w(uv) such that ∑*u N* ∈ ( ) *v wuv* ≤ 1.. The process unfolds in discrete time steps. At time t, an inactive node v becomes active if ∑*u A* ∈ ( v) w(uv) ≥ *θv* where A(v) is the set of active neighbours of v up to time-step t- 1. Also, it is a type of progressive algorithm so once a node is activated it would remain active. The diffusion process terminates when there are no more nodes remain to activate. Edge weights assigned to threshold models are either assigned with a uniform probability from the set{0.1,0.01,0.001}, or assigning each edge with a constant weight (1/din) where din is the indegree of the node.

Next famous model is independent cascade model, it considers a user v is activated by each of its incoming neighbours independently by introducing an influence probability pu,v to each edge e = (u,v). Like LT it is also a discrete optimization model and the process unfolds in discrete time steps.Each active user u in time step t will activate each of its outgoing neighbour with probability pu,v .

Each node is given a single chance to activate its outgoing neighbours. After that u stays active and stops the activation. The diffusion instance stops when no more nodes can be activated. puv parameter in the IC model is assumed to be a constant uniform edge propagation probability of 0.01 or 0.1. The influence spread of seed set S under the IC model is the expected number of activated nodes when S is the initial active node set and above stochastic process is applied.

IC and LT are all time unaware models where the diffusion terminates when no more nodes could be activated. However sometimes the propagation campaigns are time critical and requires maximizing the influence spread under a time constraint. To meet such demands, time-aware models are proposed. So the existing models can be classified as 1) discrete time step models where diffusion happens in discrete time steps 2) the continuous models where the influence spread is in continuous time. The discrete-time models [19], [20], [21] extend IC by modelling the diffusion process from one node to another as a discrete random variable over different time steps. Nevertheless, these models are essentially like IC and LT, as the diffusion only happens in discrete steps. The continuous version of Continuous-time IC considers the likelihood of pairwise propagation between nodes is a continuous distribution of time. Specifically, given the activation time tu of a node u, the conditional likelihood of u activating its neighbour v at any time tv > tu is defined as p (tu|tv; α uv)where α u,v is the parameter of a time-aware influence distribution to determine the influence strength from u to v. Given a predefined stopping time T (T > 0 ), each diffusion process stops when no more node is activated before T.

In opposition to progressive models there also exists non-progressive diffusion models. Typically, non-progressive models are SIR/SIS [22]. There also exists other model like Triggering model [24] which is a neighbouring node is activated based on the set of Triggering nodes Tv. IC and LT are all special cases of triggering model (TR).

The process of influence maximization is NP-hard under the LT, IC and TR models. Furthermore, computing the influence σ(S) of a seed set is #P-hard under the LT and IC model. [24]. So there exists greedy framework which guarantees (with approximation ration: 1 – 1/e) termination provided σ(.) is a non-negative monotone and submodular function. The algorithm is initialized with an empty seed set S, and it iteratively selects a node u into S if u provides the maximum marginal gain to the influence function σ(S) wrt. S.

Although the afore mentioned greedy framework has a good approximation ratio of (1-1/e), IM is still very challenging to solve, because evaluating σ(S) is a #P-hard problem. So various approaches have been suggested to overcome that obstacle and they are categorized based on how they overcome this P hardness. These are simulation-based approach, proxy based and sketch based. [24].

Simulation based approach utilize monte-Carlo simulation for evaluating influence spread. It starts from seed set S and traverses G by removing each edge e = (u, v) with a probability (1 - puv) until no user can be reached, resulting in a sample instance. In such a way, we can generate multiple sample instances, and the influence spread σ(S) can be estimated from the sample instances. Although this approach preserves the model generality but it has significant computational overheads.

Proxy based approach believes that the complex influence model can be effectively reduced to proxy models, e.g., PageRank or the shortest path in practice. Although being efficient it can be unstable under certain condition. [23]. Goal of goal of sketch based approach is to devise theoretically efficient solutions (instead of being only practical efficient) that also preserves a constant approximation ratio, and thus overcome the drawbacks of the above two categories of approaches. For example, the expected time complexity to get a solution in this category [15] is near linear to the size of the input graph with a constant approximation ratio[12].

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